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# Method for measuring the attenuation and phase constants of a surface wave propagating along an infinite plane

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*Indexing terms: Radar, Electromagnetic wave propagation, Electromagnetic field theory*

A method is presented for determining the attenuation and phase constants of a surface wave propagating along an infinite planar layer of metal-backed material. Two input impedance measurements of a rectangular waveguide partially filled with the test material are used to infer the propagation characteristics of the plane surface wave. Measurements are presented which validate the method.

*Introduction:* Surface waves are waves that propagate along an interface of two different media without radiation [1]. Surface wave absorbing materials are used in radar signature applications where guided waves can contribute to the radar cross-section of a vehicle. Surface wave materials are also used to minimise diffraction caused by impedance discontinuities. Many applications of these materials are associated with propagation over planar or near-planar surfaces. Characterisation of a surface wave material therefore requires a test configuration which is capable of reproducing infinite plane propagation properties without introducing other scattering or propagation mechanisms. The method adopted here uses data from a partially-filled rectangular waveguide to infer the attenuation and phase constants of the fundamental electric mode plane surface wave (components of electric field normal to the surface and in the direction of propagation).

*Theory:* If a planar perfect electrical conductor is coated with a single homogeneous and isotropic layer of material of thickness  $h$ , the propagation constant  $\beta$  of the E-mode plane surface wave is given by the solutions of the following dispersion equation:

$$\frac{\sqrt{k_1^2 - \beta^2}}{\sigma_1 + j\omega\epsilon_1} \tan\left(h\sqrt{k_1^2 - \beta^2}\right) = \frac{-j\sqrt{k_0^2 - \beta^2}}{j\omega\epsilon_0} \quad (1)$$

where  $k$ , and  $k_0$  are the TEM plane-wave propagation constants in the material and free space, respectively, and  $\sigma_1$  and  $\epsilon_1$  are the intrinsic electrical properties of the test material. If the measurement method uses planar or electrically large cylindrical surfaces to support the surface wave, it can be difficult to separate the surface wave mode from other scattering and propagation mechanisms (eqn. 1 can be shown to apply to propagation over electrically large coated cylinders). However, if the wave is constrained by the vertical and horizontal walls of a rectangular waveguide, as shown in Fig. 1, a modified surface wave mode can propagate whose attenuation and phase constants are governed by the following dispersion equation:

$$\frac{\sqrt{k_1^2 - \left(\frac{n\pi}{a}\right)^2 - \beta_m^2}}{\sigma_1 + j\omega\epsilon_1} \tan\left(h\sqrt{k_1^2 - \left(\frac{n\pi}{a}\right)^2 - \beta_m^2}\right) = \frac{-\sqrt{k_0^2 - \left(\frac{n\pi}{a}\right)^2 - \beta_m^2}}{j\omega\epsilon_0} \tan\left((b-h)\sqrt{k_0^2 - \left(\frac{n\pi}{a}\right)^2 - \beta_m^2}\right) \quad (2)$$

where  $a$  and  $b$  are the horizontal and vertical dimensions of the waveguide, respectively,  $\beta_m$  is the propagation constant of the waveguide mode and  $n$  is the waveguide mode number corresponding to rectangular type modes in the horizontal plane. Clearly  $\beta \neq \beta_m$ ; however, the only significant difference between eqns. 1 and 2 is the  $\tan$  function on the right hand side (RHS) of eqn. 2. The argument of the  $\tan$  function on the RHS of eqn. 2 is complex for surface wave modes, regardless of whether the intrinsic properties of the test material are real or complex. If the height  $b$  of the waveguide is chosen large enough as to ensure that  $\tan\left((b-h)\sqrt{k_0^2 - (n\pi/a)^2 - \beta_m^2}\right) \approx j$ , eqn. 2 becomes identical to eqn. 1 except for the known term  $(n\pi/a)^2$ . Provided  $b$  is sufficiently large, comparing eqn. 1 and eqn. 2 gives the propagation constant of a surface wave along an infinite planar layer:

$$\beta = \sqrt{\left(\frac{n\pi}{a}\right)^2 + \beta_m^2} \quad (3)$$

The accuracy of the  $\tan$  function approximation may be checked after a measurement has taken place by inserting the measured value of  $\beta_m$  into the RHS of eqn. 2.

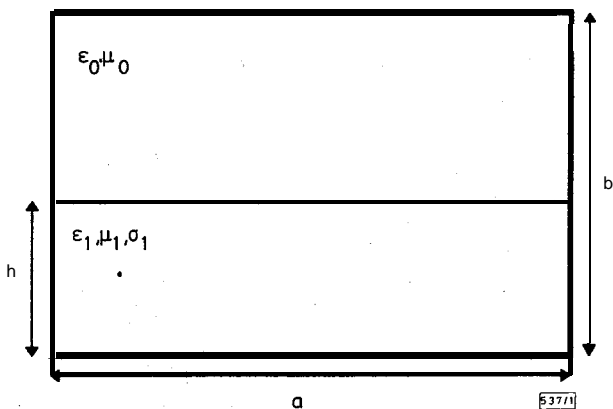


Fig. 1 Partially-filled rectangular waveguide supporting modified surface wave propagation

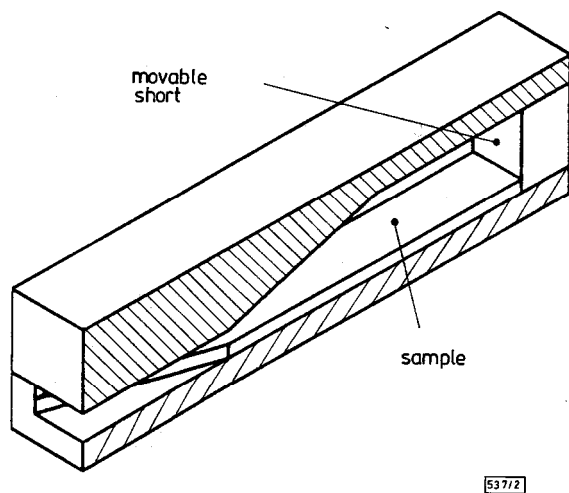


Fig. 2 Cutaway view of plane surface wave simulator cell (not to scale)

**Experimental system:** The experimental system shown in Fig. 2 is based on an X-band rectangular waveguide test cell. The test material is placed on the floor of the test cell and is tapered in the H-plane to provide a matched transition between the empty and partially-filled sections of the waveguide. The matched transition converts the fundamental empty waveguide mode ( $TE_{10}$ , i.e.  $n = 1$ ) into the fundamental modified surface wave mode. After the transition the waveguide height is increased to 34.04mm, via a taper on the upper horizontal wall of the waveguide. The partially-filled waveguide is terminated with a short circuit at the furthest end of the test cell. For many materials used in surface wave applications, analysis has shown that the  $\tan$  function approximation results in an error in  $\beta$  of  $< 1\%$ . The error can be reduced by increasing the height of the waveguide, but this has the disadvantage that the size of the test cell and the minimum sample length both increase.

Two reflection coefficient measurements are made of the uniform section of waveguide using different lengths of the shorted test cell. From these two measurements the propagation constant  $\beta_m$  can be obtained using standard transmission line theory. The reflection data are calibrated using a third measurement which defines the phase reference plane; source match and directivity errors are reduced using time domain filtering. The length of the test cell is chosen to ensure that the time domain response of the sample is isolated from the two error responses. When  $\beta_m$  has been measured, the infinite plane surface wave absorption and phase constants are obtained from eqn. 3.

**Results:** Measurements have been performed using high molecular weight polyethylene. Material thicknesses of 3.25 and 6.15mm

were used. Because polyethylene has very low losses, only results relating to the phase constants have been calculated. The measurement of lossy materials is made marginally easier by the reduction in the magnitude of the source match error. Fig. 3 shows the measured and predicted phase constants for a fundamental mode plane surface wave supported by an infinite planar layer of 3.25 and 6.15mm metal backed polyethylene. The results show good agreement between measured and predicted values. Owing to the higher impedance mismatch between the empty and partially-filled sections of waveguide, an increase in ripple is seen in the data for the 6.15mm sample. However, improved tapering between the empty and partially-filled sections of X-band waveguide would reduce this error.

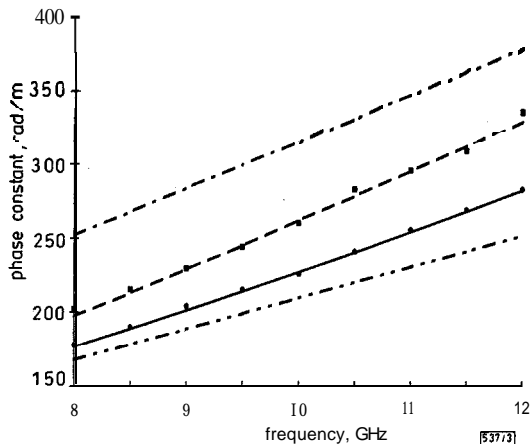


Fig. 3 Measured and predicted phase constants for fundamental electric mode plane surface wave supported by infinite planar sheet of metal-backed polyethylene

**Conclusions:** A method has been developed for measuring the attenuation and phase constants of a fundamental mode plane surface wave propagating along an infinite planar layer of metal-backed material. The method can be used to characterise the surface wave absorbers used in radar signature applications. The dimensions of the test sample depend on the waveguide band under investigation; in the case of the X-band test cell the minimum sample dimensions are 22.86 x 300mm<sup>2</sup> (the larger dimension is approximate). There exists a small inherent inaccuracy in the method due to confinement of the surface wave by the upper horizontal wall of the waveguide; however, the inaccuracy can be detected in the measured data and minimised, if necessary, using alternative cell dimensions. The cell has been designed to interrogate the fundamental electric mode plane surface wave. A similar approach can be used to interrogate the fundamental magnetic mode plane surface wave.

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